INTEGRAL FORCE/MOMENT WATERJET MODEL FOR CFD SIMULATIONS

Manivannan Kandasamy, Seng Keat Ooi, Pablo Carrica, Frederick Stern
IIHR-Hydroscience & Engineering
The University of Iowa
Iowa City, IA 52242

Abstract

An integral force/moment waterjet model for CFD is derived for ship local flow/powering predictions, including sinkage and trim. The waterjet induced reaction forces and moment and waterjet/hull interaction stern force replicate the effects of the waterjet without requiring detailed simulations of the waterjet system. The model extends the ITTC waterjet model for sinkage and trim by using an alternative control volume also appropriate for CFD and by including vertical forces and pitching moment in the waterjet/hull force/moment balance. The same grid is used for both without and with waterjet simulations. The CFD waterjet model requires limited waterjet geometry (inlet and outlet areas and locations; and weight of working fluid) and several waterjet flow (mass flow rate; inlet pressure force; inlet and outlet momentum correction factors and flow angles; and stern force and location) input variables. The CFD waterjet model can be used for local flow predictions by using waterjet flow input variables provided by ITTC waterjet model test data, including additional data for waterjet induced inlet pressure and stern forces. It can also be used for powering predictions once waterjet flow input variable correlations are available based on CFD for the waterjet system and/or experimental data. The CFD waterjet model is demonstrated for local flow predictions for the DTMB 5594 high-speed sealift ship model for which ITTC waterjet model test data, including additional data for waterjet induced stern forces are available. Correlations for the waterjet flow input variables are shown to be feasible using combination of CFD and experimental data for the waterjet system for three different hulls.
1. Introduction

Waterjet propulsion systems are increasingly being used for high-speed ships. Most CFD is for the waterjet system alone without considering waterjet/hull interaction or powering prediction due to the difficulty of geometry modeling and grid generation for the combined ship and waterjet system, as reviewed by the Report of the 24th ITTC Specialized Committee on Validation of Waterjet Test Procedures [1]. Stern et al. [2] demonstrated CFD capability for simulating waterjet self-propelled high-speed trimaran sealift ships including above water discharge in both calm water and irregular head waves at sea state 6 conditions using CFDShip-Iowa [3]. Kandasamy et al. [4] carried out detailed validation of the waterjet performance predictions for the Joint High Speed Sea-Lift (JHSS). However, for some applications, details of the waterjet induced flow are not required and a simplified force/moment waterjet model is desirable, conceptually similar to that developed previously for propeller propulsion systems [5]. The current study was motivated by the need to model the waterjet’s effect on the trim of high-speed, low-wake, semi-planning passenger ferries cost effectively during the initial design stages, as the trim affects both the resistance and wake height significantly [6].

The ITTC [1] has developed waterjet test procedures, which combine model testing with control volume/integral analysis for ship powering predictions hereafter referred to as ITTC waterjet model. Herein, an integral force/moment waterjet model for CFD is derived for ship local flow/powering predictions, including sinkage and trim. The waterjet induced reaction forces and moment and waterjet/hull interaction stern force replicate the effects of the waterjet without requiring detailed simulations of the waterjet system. The model extends the ITTC waterjet model for sinkage and trim by using an alternative control volume also appropriate for CFD and by including vertical forces and pitching moment in the waterjet/hull force/moment balance. The same grid is used for both without and with waterjet simulations. The CFD waterjet model requires limited waterjet geometry (inlet and outlet areas and locations; and weight of working fluid) and several waterjet flow (mass flow rate; inlet pressure force; inlet and outlet momentum correction factors and flow angles; and stern force and location) input variables. The CFD waterjet model can be used for local flow and sinkage and trim predictions by using waterjet flow input variables provided by ITTC waterjet model test data, including additional data for
waterjet induced inlet pressure and stern forces. It can also be used for powering predictions once waterjet flow input variable correlations are available based on CFD for the waterjet system and/or experimental data. The CFD waterjet model is demonstrated for local flow predictions for the DTMB 5594 high-speed sealift ship model for which ITTC waterjet model test data, including additional data for waterjet induced stern forces are available. Correlations for the waterjet flow input variables are shown to be feasible using CFD for the waterjet system for three different hulls.

2. ITTC Waterjet Model

The ITTC waterjet model combines model testing with control volume/integral analysis for ship powering predictions. Such procedures are required due to difficulties for direct measurement of the waterjet net thrust.

The ITTC waterjet model control volume set in the carriage-fixed inertial frame of reference, shown in Fig. 1, was selected for the waterjet system in order to be able to compute or determine the powering characteristics from measurements, with consideration to (1) ease of measurement of momentum and energy fluxes across inlet and outlet, (2) control volume boundaries capture all inflow and outflow of waterjet system, and (3) the protruding part of the control volume defined by surface ABC should be as small as possible to avoid strong interaction effects with the external flow. The selected control volume is defined by a streamtube consisting of the nozzle, pump, ducting system, inlet, and upstream imaginary surface BC in the flow through which it is assumed no mass transport occurs by definition with one outlet A6 and inlet A1A. Vertical reaction force, weight of the working fluid, and pressure and shear forces acting on BC are neglected. The inlet A1A is selected to avoid major flow distortions by the intake geometry and as practical choice is usually one impeller diameter in front of the ramp tangency point.

The ITTC model procedures provide a series of standardized tests for the prediction of the main powering characteristics such as power-speed and impeller rotation rate-speed relation. The procedures are presented in global terms leaving sufficient freedom for individual institutes to
use their own preferred methods. The first step is the collection of data such as nozzle area, $A_6$, hull length $L_{pp}$ and static wetted surface area $A_S$.

The second step is the resistance test and wake-field measurements where a resistance test is carried out for a bare hull model with closed intakes that is free to sink and trim. The total bare hull resistance $R_{TBH}$ is obtained and is used later to estimate the thrust deduction factor, $t$. During the resistance test the boundary layer velocity profile $u_{1Ax}(y,z)$ is measured at Station 1A. This profile will be used later to calculate the following items: the intake area at station 1A, the average velocity at station 1A, $\bar{V}_{1A}$, and the momentum correction factor at Station 1A, $c_{mi}$, which is calculated at any station N using Eq. (1-2)

$$c_{MN} = \frac{1}{A_N} \int_{A_N} \left( \frac{u}{\bar{V}_N} \right)^2 dA$$  \hspace{1cm} (1)

$$\bar{V}_N = \frac{1}{A_N} \int_{A_N} (\mathbf{V} \cdot \mathbf{n}) dA$$  \hspace{1cm} (2)

The third step is the calibration and propulsion test. The purpose of the calibration test is to establish a relation between a measurement signal at the jet (often a differential pressure transducer or Kiel probe is used) and the jet-thrust ($T_{Jx}$) which is measured through the Bollard pull test. The flow rate ($Q$) is then calibrated through the momentum flux approach, since direct measurement of flow-rate is prone to higher uncertainties. Assuming negligible inlet axial velocity, $T_{Jx}$ is equal to the momentum flux at the jet nozzle providing Eq. (3) for estimating $Q$.

$$Q = \sqrt{\frac{T_{Jx} A_6}{\rho c_{m6} \cos \alpha}}$$  \hspace{1cm} (3)

During the calibration phase, the momentum correction factor at the jet exit $c_{m6}$ is obtained from detailed jet velocity profiles using LDV. $\alpha$ is the jet angle relative to the horizontal at the nozzle (station 6). This calibration is assumed to hold good even with non-zero forward velocity, so that the Kiel probe measurements taken during self-propulsion tests could be used to estimate $Q$. 
After calibration, the propulsion test is carried out to determine relation between speed, flow-rate and thrust at self propulsion point. Note that the ITTC model procedure recommends that the self-propulsion point be determined through thrust identity which requires that the non-dimensional thrust loading be the same in both full and model scale. The model must then be towed with a make-up added tow force to account for the higher friction in model scale due to the thicker boundary layer which is defined as

\[ F_D = \frac{1}{2} \rho U_o^2 S (C_{Fm} - C_{Fs}) \]  

(4)

where \( U_o \) is the desired model velocity, \( S \) is the model wetted surface area, \( C_{Fm} \) and \( C_{Fs} \) are the model and ship friction coefficients, calculated from the ITTC ship-model correlation.

The calibrated Kiel probe measurements provide \( Q \) at the self-propulsion point. \( Q \) is then used to determine the size of the inlet capture area from the inlet wake-field measurements by applying conservation of mass. Once the capture area is determined \( c_{ml} \) can be calculated. All the relevant variables to predict the waterjet net thrust \( (R_X) \) from Eq. (5) are now known.

\[-R_X = \rho Q^2 A_6 c_{M6} \cos \alpha - \rho Q c_{Min} U_o \]  

(5)

Which can alternatively be written as in Eq. (6)

\[ R_X = -m \left( c_{M6} \bar{V}_{6X} \cos \alpha - c_{Min} \bar{V}_{inX} \right) \]  

(6)

Notice that the ITTC model ignores vertical forces and pitching moments needed to evaluate sinkage and trim in a CFD simulation. These are not relevant for the purposes of the original ITTC model, since sinkage and trim are measured during the thrust evaluation procedure. For a CFD simulation, however, it is desirable to estimate the resulting waterjet-induces forces and moments affecting sinkage and trim, since the final attitude of the ship affects the resistance and wave-generation characteristics of the ship.
3. CFD Waterjet Model

The purpose of the CFD waterjet model is for ship local flow/powering predictions including sinkage and trim without requiring detailed simulations for the waterjet system (nozzle, pump, ducting system, and inlet). The control volume shown in Fig. 2 is selected with consideration to (1) implementation simplicity in CFD using same grid as for without waterjet simulations by representing the waterjet system by axial and vertical reaction forces and pitching reaction moment, and by representing the waterjet/hull interaction using a vertical stern force, (2) ability to predict either speed for given powering or vice versa including sinkage and trim, and (3) require as limited number of empirical correlations as possible. The selected control volume is similar to the ITTC model, except the imaginary surface BC in the flow is removed and the inlet is taken as the actual inlet to the waterjet across the bottom plane of the hull. The flow angles with respect to the keel at the intake and nozzle are $\phi$ and $\alpha$, respectively. The waterjet induced forces on the control volume are, $\Delta P_{in}A_{in}$, the change in pressure force on the hull at the location of the intake, and $\Delta W_f$, the weight of water in the waterjet dead volume. The waterjet induced pressure at the outlet is usually small; therefore, not included, but can easily be incorporated.

The choice of the proposed control volume for the waterjet instead of the ITTC control volume is also motivated by the possibility of experimentally measuring the pressure and velocities at the waterjet inlet, which allows for the computation of the inlet flow angle $\phi$, momentum flux correction factor $C_{Min}$, pressure force $\Delta P_{in}A_{in}$, and pressure distribution at stern which provides the waterjet/hull interaction stern force $\Delta F_S$. The ITTC control volume is limited by a streamtube entering the waterjet duct; determining the limiting streamlines forming the streamtube and measuring pressures on its surface for the purposes of calculating vertical forces and pitching moments would be extremely difficult. Also, curved streamlines near the waterjet inlet point to strong pressure gradients, an additional indication that neglecting those pressure forces would be questionable.

Figure 3 shows the coordinate systems, forces and moments for towed bare hull (Fig. 3a) and towed waterjet-propelled (Fig. 3b) ship models in a ship-fixed reference frame which uses
(X,Y,Z) coordinates, moving with constant velocity \((-U_0,0,0)\) in the relative inertial frame. The model ship is assumed free to sink and trim. The origin is located at the center of gravity \(CG=(x_{CG},y_{CG},z_{CG})\) with the CG coordinates expressed in the usual absolute inertial CFD system \((x,y,z)\) with \(x=0\) located at the forward perpendicular of the ship at rest condition in calm water with \(x\) positive downstream and \(z=0\) at the calm water plane with \(z\) positive upward and the \(y\) coordinate pointing to starboard, forming a right hand system. The area shaded in grey in Fig. 3b shows the control volume for the waterjet model in the self-propelled ship. For convenience, the control volume analysis for the waterjet propelled case uses Cartesian coordinates similar to \((X,Y,Z)\), but with origin at the thrust bearing and position vector \(r_R\) relative to the CG, as shown in Figs. 3. The thrust bearing defined by a vector \(r_r\) from the CG (see Fig. 3b) is not necessary for the derivation of the waterjet model but is used because it makes the model conceptually easier to derive. Position vectors are defined from the thrust bearing to the intake \(r_{in}\), to the nozzle \(r_6\) and to the centroid of the weight of the fluid in the waterjet \(r_{AWf}\).

### 3.1 Integral Waterjet Force/Moment Analysis

The reaction forces and moment \(M_{RY}\) about the thrust bearing are obtained using the Reynolds transport theorem with the ship-fixed, non-deforming control volume, for steady, incompressible flow.

At the inlet

\[
\vec{V}_m = \vec{V}_m \cos \phi \hat{i} + \vec{V}_m \sin \phi \hat{k} = \vec{v}_{inX} \hat{i} + \vec{v}_{inZ} \hat{k}
\]  

(7)

and at the outlet

\[
\vec{V}_6 = \vec{V}_6 \cos \alpha \hat{i} + \vec{V}_6 \sin \alpha \hat{k} = \vec{v}_{6X} \hat{i} + \vec{v}_{6Z} \hat{k}
\]  

(8)
The conservation of linear momentum gives the reaction force

\[- \mathbf{R} = \dot{m} \left( c_{M6} \overline{V}_6 - c_{Min} \overline{V}_{in} \right) - \Delta P_{in} \mathbf{A}_{in} + \Delta \mathbf{W}_f \]  

Eq. (9) is decomposed into axial and vertical components, as follows:

\[ R_X = -\dot{m} \left( c_{M6} \overline{V}_{6X} - c_{Min} \overline{V}_{inX} \right) + \Delta P_{in} A_{inX} - \Delta \mathbf{W}_{fX} \]  

\[ R_Z = -\dot{m} \left( c_{M6} \overline{V}_{6Z} - c_{Min} \overline{V}_{inZ} \right) + \Delta P_{in} A_{inZ} - \Delta \mathbf{W}_{fZ} \]  

Eq. (10) reduces to Eq. (6) if $\Delta P_{in} A_{inX}$ can be neglected and also $\Delta \mathbf{W}_{fX} = 0$. Note that the sign of $\Delta P_{in} A_{inX}$ term may change depending on the orientation of vector $\mathbf{A}_{in}$.  

The conservation of angular momentum gives reaction pitching moment about the thrust bearing $M_{RY}$

\[ M_{RY} = \left( -\dot{m} (\mathbf{r}_6 \times c_{M6} \mathbf{V}_6 - \mathbf{r}_{in} \times c_{Min} \mathbf{V}_{in}) + (\mathbf{r}_6 \times \Delta P_{in} \mathbf{A}_{in}) + (\mathbf{r}_{AWj} \times \Delta \mathbf{W}_f) \right) \cdot \mathbf{j} \]  

3.2 Waterjet/hull Force/Moment Balance

The force and moment of the waterjet system on the ship is obtained from the equilibrium of forces and moments on the ship using the ship-fixed (X,Y,Z) coordinate system, as shown in Fig 3a,b for the without and with waterjet conditions, respectively. CFD simulations provide the hydrodynamic forces $\mathbf{C}_T = (C_{TX}, 0, C_{TZ})$ and moment $M_{TY}$ transformed into the (X,Y,Z) coordinate system.

Equilibrium of forces and moments for the waterjet-propelled condition requires that
\[
\sum F_x = C_{TX} + R_x + \Delta F_{sx} - F_D \cos \tau - W \sin \tau = 0
\] (13)

\[
\sum F_z = C_{TZ} + R_z + \Delta F_{sz} - W \cos \tau - F_D \sin \tau = 0
\] (14)

\[
\sum M_y = M_{RY} + (r_r \times R) \cdot \mathbf{j} + (r_{\Delta FS} \times \Delta F_S) \cdot \mathbf{j} + M_{TY} = 0
\] (15)

\(F_D\) is the added tow force in the axial direction of the carriage, \(W\) is the weight of the ship, 
\(r_{\Delta FS} = (X_{FS}, 0, Z_{FS})\) is the position vector from the CG to \(\Delta F_S\), and \(\tau\) is the trim angle. Expanding Eq. (15) results in

\[
\sum M_y = M_{wJ} + M_{TY} = 0
\] (16)

where

\[
M_{wJ} = M_{RY} + Z_R (R_x) - X_R (R_z) + Z_{FS} (F_{sx}) - X_{FS} (F_{sz})
\] (17)

Eqs. (13) to (17) can also be used for the towed bare hull simulations by setting all the waterjet forces \(R_x, R_z, F_{sx}, F_{sz}\), moments \(M_{RY}, M_{wJ}\) and position vectors \(r_{\Delta FS}, r_r\) in the equations to zero.

In summary, the CFD waterjet model includes vertical reaction force, weight of the working fluid, pressure forces acting on the inlet, and pitching moment. Additionally, the waterjet/hull interaction is represented by a waterjet induced stern force, which is included in the waterjet/hull force/moment balance. The input variables required are: for geometry \(A_{in}, A_6, r_r, r_{in}, r_6, r_{\Delta WJ}\), and \(\Delta W_i\); and for waterjet flow \(\dot{m}, \Delta P_{in} A_{in}, c_{Min}, c_{M6}, \phi, \alpha\), and \(\Delta F_S\). For current validation of the waterjet model, these input variables are acquired from experiments on DTMB 5594. The feasibility of acquiring these input variables from correlations is discussed in Section 6.
4. Computational Method

The waterjet model was implemented in CFDShip-Iowa version 4.0. CFDShip-Iowa version 4.0 [3] makes use of a single-phase level set method, advanced iterative solvers, conservative formulations, and dynamic overset grid approach for simulating 6DOF ship motions in free surface viscous flows. The code has been validated for various cases of which the most relevant are for DTMB 5512 pitch and heave [7], high speed towed and self-propelled simulations of R/V Athena [8], and high speed (Fr > 0.4) sealift ships in various conditions [2]. The results are summarized in Table 1.

The fluid and the rigid multi-body systems of equations can be solved in either an absolute inertial system (the earth system) or in a relative inertial system moving at the constant ship forward speed (the towing tank carriage system). This allows the use of several moving ships and within each ship the use of rotating propellers and rudders. For the current case, a relative inertial system was used where the forces and moments are computed on the relative inertial system, and then projected into the local non-inertial system of coordinates, i.e. the ship-fixed reference frame, to solve the rigid-body equations and obtain the motions. Once the new positions of the moving objects are known, the grids are displaced and the grid point velocities are used as boundary conditions for the non-slip surfaces.

The computational domains extend from $-0.5 < x < 2.0$, $0 < y < 1.0$, $-1 < z < 0.25$, in dimensionless coordinates based on $L$. Boundary conditions are shown in Table 2. Taking advantage of the problem symmetry, a half-domain overset grid as shown in Fig. 4 was used with 1.4 million grid points for the body-fitted ship grid and 400,000 grid points for the Cartesian background grid. The grid design and number of points were deemed adequate for present purpose based on previous verification studies for similar geometry and conditions. Computational grids for the hull were designed to accurately resolve geometric features of the model and the unsteady turbulent boundary layer, wake, and wave fields. The grids were generated using GRIDGEN. The hull boundary layer has a double-O topology and was created with a hyperbolic grid generator, with a grid spacing at the hull designed to yield $y^+ < 1$. This grid was free to move with the ship.
3-5 inner iterations were used for convergence of the flow field equations within each time step. Convergence of the pressure equation is reached when the residual imbalance of the Poisson equation drops six orders of magnitude. All other variables are assumed converged when the residuals drop to $10^{-5}$.

5. Demonstration and Validation of WJ model for 5594

The CFD waterjet model was demonstrated and validated with simulations for the DTMB 5594 high-speed sealift ship model for which waterjet geometry and most flow input variables are available from experiments [9]. The validation data is for $Fr = U_0 / \sqrt{gL_0} = 0.511$ and $Re = U_0 L_0 / \nu = 2.9 \times 10^7$. Global and local flow measurements were made for bare hull resistance and self propelled conditions. The net waterjet thrust was estimated using the ITTC waterjet recommended procedures and guidelines. Local flow measurements include: axial velocity contours upstream of the inlet and surface pressure distribution over the stern downstream, between, and upstream of the inlet for both without and with waterjet conditions; and all required ITTC waterjet input variables.

For validation purposes, in consideration of the available experimental fluid dynamics (EFD) benchmark data, the CFD waterjet model was implemented with towed propelled condition, i.e., with prescribed speed and waterjet induced vertical reaction force and moment. The resistance, sinkage and trim were predicted. Since the ship model is at the self-propulsion point the difference between EFD $R_X$, sinkage, and trim and CFD $C_{TX}$, sinkage and trim provides an assessment of the capability of the CFD waterjet model. Simulations and comparisons with EFD are also done for the bare hull condition; thereby, providing an assessment of the prediction of waterjet induced changes.

5.1. Evaluation of CFD Waterjet Model Input Variables for 5594

Wilson et al. [9] provided the waterjet flow variables $R_X$, $\dot{m}$, $c_{M6}$, and $\Delta F_S$; and most of the geometry $A_{in}, A_6, r_R, r_m, r_6, \alpha$ was assumed zero, as per the waterjet geometry. Detailed surface
grid information and preliminary CFD solutions for the same geometry and conditions, including waterjet system, provided $r_{swf}$, $\Delta W_t$, and $c_{Mn}$ [10]. The required input parameter $\phi$ was unavailable. Hence $R_X$ was used to estimate $\phi$ by control volume analysis as follows.

Since $\alpha=0$, $\bar{V}_{6z} = 0$ and applying conservation of mass at exit gives

$$\bar{V}_{6x} = \frac{m}{\rho A_6} = 1.47U_0$$  \hspace{1cm} (18)

Solving Eqn. (10) gives $\bar{V}_{inX} = 0.730U_0$. Applying conservation of mass at the horizontal inlet gives

$$\bar{V}_{inz} = \frac{m}{\rho A_{inz}} = 0.216U_0$$  \hspace{1cm} (19)

The angle $\phi$ is obtained from Eq. (20)

$$\phi = \tan^{-1}\left(\frac{\bar{V}_{inz}}{\bar{V}_{inX}}\right) = 16.45^\circ$$  \hspace{1cm} (20)

which is shallower than the geometrical angle of the waterjet inlet $\phi' = 27^\circ$. If the geometrical angle $\phi' = 27^\circ$ was used as an approximation for the inflow angle $\phi$, the resulting $R_X$ would be 7% larger than EFD.

Detailed pressure measurements were taken by Wilson et al. [9] on the stern of the model. The measurements were made across the width and length of the stern and in both directions included points surrounding the intakes, but not in the intake itself. It was decided to estimate the pressure at the intake from the closest measurement points and the distributions of pressure measurements surrounding the intake. The detailed measurements were provided as non-dimensional pressure
coefficients $C_p$ measured longitudinally along the centerline of the hull and the port-side of the hull for both active and inactive waterjet conditions.

$$C_p = \frac{P - P_o}{\rho U_o^2} \quad (21)$$

The difference in $C_p$ between active and inactive waterjet conditions at the centerline of the hull and the port-side of the hull was then averaged to get the longitudinal distribution of $\Delta C_p$ along the stern (Fig. 5). This longitudinal distribution is assumed to hold over the total stern area $A_{TZ}$.

The total stern force $\Delta F_{TZ}$ is obtained as

$$\Delta F_{TZ} = \Delta F_{Sz} + \Delta P_{in} A_{inZ} = \iint_{A_{TZ}} \Delta C_p da \quad (22)$$

Table 3 summarizes the non-dimensional CFD waterjet model input variables for the current implementation and values used to non-dimensionalize the input variables are tabulated in Table 4.

The CFD waterjet model reaction forces/moments and their components are summarized in Table 5. Based on the current assumptions/implementation the axial reaction force $R_x = -8.767 \times 10^{-5}$. The waterjet induced stern force $\Delta F_{TZ}$ is negative and more than twice as large as the vertical momentum flux $M_Z$.

$$M_Z = \dot{m} c_{MinZ} \bar{V}_{inZ} \quad (23)$$

The overall waterjet induced vertical force is negative and equals $-3.6 \times 10^{-5}$. The waterjet induced pitching moment about the CG is positive, i.e., positive trim predominantly due to moment of $\Delta F_{TZ}$ and small contribution from moment of $R_x$. 
5.2 Validation of Global Variables

Simulations were conducted for both towed barehull and towed propelled conditions and the resistance, sinkage, and trim were predicted. The error in predicted total resistance ($C_{TX}$) for the towed bare hull simulation (Table 6) is $E=0.78\%$, where the relative error $E$ is defined as $E(\%D)=|EFD-CFD|/EFD \times 100$. The error in sinkage is $E=0.8\%$ and trim is $14.3\%$. The errors are within the range of error values obtained from this code in previous simulations (Table 1). For the towed propelled simulations the error for resistance, sinkage and trim are $-4.6\%$, $9.0\%$, and $13.6\%$, respectively.

Waterjet induced changes in sinkage and trim were estimated using hydrostatics approximations [11]. The hydrostatic heave restoring force is written as the incremental heave for an incremental restoring force:

$$\Delta \sigma = \frac{R_E}{\rho g A_{wp}}$$  \hspace{1cm} (24)

where $\Delta \sigma$ is the induced sinkage due to the waterjet, $\rho$ is the density of water and $A_{wp} = 0.0509L_0^2 = 2.4631m^2$ is the waterplane area [10]. The standard moment to trim one degree was modified to account for any small incremental angle instead of one degree. This results in the following expression

$$\Delta \tau \approx \sin^{-1}(M_{wj}/\rho g I_L)$$  \hspace{1cm} (25)

where $\Delta \tau$ is the waterjet induced change in trim angle, $I_L$ is the longitudinal moment of inertia about the center of flotation. The results are summarized in Table 7.

Table 7 includes CFD predictions of waterjet induced sinkage and trim. The E=-58\%D and 11.5\%D for $\Delta \sigma$ and $\Delta \tau$ are larger than the hydrostatic estimates. Table 7 also shows the relative induced change in sinkage $\Delta \sigma/\sigma_{BH}$ and trim $\Delta \tau/\tau_{BH}$ which serves as a better measure of the waterjet/hull interaction than $\Delta \sigma$ and $\Delta \tau$. The towed bare hull CFD simulation values of
sinkage $\sigma_{BH}$ and trim $\tau_{BH}$ are used in the computation of $\Delta \sigma / \sigma_{BH}$ and $\Delta \tau / \tau_{BH}$ for the CFD predictions. The CFD waterjet model under predicts $\Delta \sigma / \sigma_{BH}$ as $\Delta \sigma / \sigma_{BH} = 7.01\%$ compared to the EFD value of 16.97\%, for $\Delta \tau / \tau_{BH}$ the CFD waterjet model predictions are reasonable as $\Delta \tau / \tau_{BH} = 25.51\%$ compared to $\Delta \tau / \tau_{BH} = 24.57\%$ reported by EFD.

The large relative induced change in sinkage and trim show that the waterjet/hull interaction is significant. However, because the absolute magnitudes of the induced sinkage and trim are small, the change in resistance between the towed bare-hull and towed propelled models at the same speed is small. This result indicates that for this displacement ship at this Froude number the change in sinkage and trim due to the waterjet/hull interaction will not affect speed significantly for the same power.

### 5.3 Validation of Local Variables

The primary purpose of implementing the waterjet model using waterjet model input data from experiments is that flow details like boundary layer profiles, bow/sonar-dome vortices, and wave elevations, which are expensive to obtain from experiments, can be obtained through the simulations. This is especially true when farfield wave elevation are required, which in some cases are highly sensitive to waterjet induced changes in trim angle. Wave elevation data is unavailable for the 5594 self propelled cases. Here, the predictive capability of CFDShip for local flow variables is demonstrated in Fig. 6, which shows the nominal wake contours of the non-dimensional axial velocity immediately upstream of the waterjet inlet ($x/L=0.93$) with the inlets closed and the model towed at a fixed sinkage and trim condition equal to that of the self-propelled case. The CFD contours show a good agreement with the EFD [9], with a slight over prediction of the boundary layer thickness.

### 6. Correlations for CFD Waterjet Model

Ultimately, the waterjet model will be of most use if general correlations can be obtained, which would provide the water-jet flow input variables. Recently, detailed self-propulsion simulation
of waterjet appended ships have been performed, which provide opportunity to investigate if such correlations are feasible. Kandasamy et al. [4] provide detailed self propulsion simulation results for waterjet appended Joint High Speed Sea-lift (JHSS). The results were validated using experimental data [12]. In addition, simulation results are also available for Delft catamaran (DC) for which experimental results for validation are available from ongoing ONR collaborative project with Bulgarian Ship Hydrodynamics Centre [13]. In this section, we explore the possibility of obtaining suitable correlations from self propulsion simulations for JHSS and DC, along with the experimental data available for 5594.

Figure 7a shows the barehull resistance $C_{TX}$ and self propelled net jet thrust $R_X$ for both the experiments and the simulations. Detailed waterjet self-propelled simulation results are available in the range $0.18 < Fr < 0.39$ for JHSS and $0.46 < Fr < 0.80$ for DC, along with validation data. Barehull validation data is available for DC over a wider range $0.20 < Fr < 0.70$. $R_X$ is available for 5594 only at $Fr=0.511$, and $C_{TX}$ is available over the whole range $0.20 < Fr < 0.80$. From the simulation results, $R_X$ for JHSS and DC was obtained using the CFD waterjet model control volume and is within $\pm 2\%$ of the values obtained using the ITTC control volume. A log scale is used in the plots since $C_{TX}$ and $R_X$ values for DC are up to an order of magnitude higher than JHSS and 5594 for the following reasons: 1) The non-dimensionalization parameter is $L^2$, and being a catamaran in addition to having a lower demihull slenderness ratio than the other two hulls, the wetted surface area to $L^2$ ratio for DC is almost four times larger than JHSS and 5594 and 2) the values for DC are at model scale, whereas JHSS and 5594 were investigated with full-scale thrust identity and added tow force. In Fig. 7a, the added tow force has been subtracted from the barehull $C_{TX}$ for JHSS and 5594 to enable comparison with $R_X$ and for the calculation of thrust deduction fraction $t$.

For DC, $C_{TX}$ and $R_X$ are within $3.9\%$ and $9\%$ of the benchmark data, respectively. For JHSS, $C_{TX}$ and $R_X$ are within $6.2\%$ and $7.1\%$ of the data, respectively. Both DC and 5594 show the characteristic $C_{TX}$ hump at $Fr\sim0.5$, but it is more prominent for DC. Data is not available for JHSS at the hump region. The simulations show a reasonably good agreement with data for the thrust deduction fraction $t$ (Fig. 7b). The experiments show a negative thrust deduction for 5594 at $Fr=0.51$; simulations are not available for this condition. Figure 7c shows the sinkage for the
different hulls. For both DC and JHSS, simulations and experiments show negligible effect of the waterjet on the sinkage, and the simulation results corresponds well with the data. The waterjet induced increase in trim (Fig. 7d) is highest for DC, moderate for 5594, and comparatively negligible for JHSS. The simulation and experimental trim values compares well for both DC and JHSS.

The transom vertical force components for the different hulls over the Fr range shown in Fig. 8a show similar trends as $R_X$ in Fig. 7a. DC vertical forces are almost an order of magnitude greater than JHSS and 5594, and peak at Fr~0.5, similar to $R_X$. For JHSS, both the vertical forces and $R_X$ indicate a gradual rise after Fr=0.3. The inlet velocity ratio (IVR), which is $\frac{V_{Ain}}{U_0}$ from Eq. (2) normalized by the free stream velocity $U_0$ is plotted alongside and also shows similar trends as the vertical force components. Plotting the vertical forces against the IVR (Fig. 8b) indicates a noticeable log-linear trend between the vertical forces and IVR for both JHSS and DC. Since the vertical forces for DC is about an order of magnitude greater than the other two hulls, a generalized correlation between the vertical force components and the IVR that can encompass all the hulls is unattainable. Fig. 8c shows the relative contributions of $\Delta P_{inA_{inZ}}$ and $\Delta F_{SZ}$ by plotting the ratio $\Delta P_{inA_{inZ}}/\Delta F_{SZ}$ against IVR. The differences in the waterjet inlet and hull designs account for the dominance of $\Delta P_{inA_{inZ}}$ component in JHSS and $\Delta F_{SZ}$ component in DC. For both hulls, the contribution of $\Delta P_{inA_{inZ}}$ component increases with increasing IVR.

Fig. 9a and 9b give the variation of $\phi$ and $\phi/\phi'$ vs. IVR, respectively. A linear least square fit (LSF) over the data for $\phi$ over all the points is possible with a correlation coefficient ($R^2$) of 0.98. The variation in $\phi/\phi'$ is small, between 0.5 - 0.6, for the different ships over the IVR range and a linear LSF gives $R^2=0.82$. Fig. 10 shows the momentum correction factors the waterjet inlet vs. IVR. A LSF with a second order polynomial gives $R^2$ values of 0.98 for both $C_{MinX}$ and $C_{MinZ}$. $C_{M6}$ at outlet is almost constant ~ 1.03±2%.

Noting that both $C_{TX}$ and $-F_{TZ}$ for DC are almost an order of magnitude higher than the other two hulls, a general correlation for the vertical forces to encompasses all the different hull/waterjet designs seems possible, by plotting the ratio $-F_{TZ}/C_{TX}$ against IVR (Fig. 11). This ratio is similar to the lift/drag coefficients used in aerospace engineering. $C_{TX}$ is used here instead of $R_X$, since
$R_X$ will be unavailable during implementation of the waterjet model for predictive purposes. A logarithmic LSF fit over all the hulls is possible with $R^2=0.95$. Note that $\Delta P_{in}A_{inZ}$ for 5594 was approximated by the closest pressure measurements at the stern and is not an accurate representation of its true value as evident from Fig. 8c. A logarithmic LSF fit with $R^2=0.98$ is possible if only JHSS and DC are considered.

These correlations provide all the waterjet inlet flow variables as a function of $IVR$. Eq. 10 can be re-written as functions of $IVR$ as follows

$$R_X = fn(IVR) = -IVR^2 \times A_{inZ} \left( c_{M6} \frac{A_{inZ}}{A_{bX}} - c_{MinX} \cot \phi \right) \tag{26}$$

As an initial guess, the waterjet geometric angle information can be used to get an estimate of the inflow angle assuming inflow/geometric angle ratio~0.55. The corresponding $IVR$ is obtained from Fig. 10b. For a particular Fr, based on $C_{TX}$ and the initial $IVR$ estimates, the total vertical stern force is calculated using the correlation from Fig. 11, which provides $\Delta F_{TZ}$ and the vertical momentum flux term is obtained as

$$M_Z = IVR^2 \times A_{inZ} \times c_{MinZ} \tag{27}$$

A towed propelled simulation can be conducted at the particular Fr to obtain a new $R_X$. $IVR$ is then recalculated from Eq.26. $c_{MinZ}$ is recalculated for the new $IVR$, and $M_Z$ is obtained from Eq.27. The vertical forces are recalculated based on the new $IVR$ from Fig. 11, and the steps are iterated until convergence.

6. CONCLUSIONS

An integral force/momentum waterjet model for CFD is derived for ship local flow/powering predictions, including sinkage and trim. The CFD waterjet model is derived in a ship-fixed reference frame and extends the ITTC waterjet model by using a control volume appropriate for CFD, which includes vertical forces $R_Z$ and angular momentum $M_{RY}$. In addition, the model
accounts for the waterjet-hull interaction by incorporating a stern force $\Delta F_S$ in the balance of forces and moments for the ship. This allows the CFD waterjet model to predict sinkage and trim in addition to resistance for waterjet-propelled ships without requiring detailed modeling of the waterjet geometry.

The model is demonstrated and validated using existing data from towing tank experiments of a towed bare-hull and towed propelled DTMB 5594 using $R_x$ from EFD as an input parameter to estimate $\phi$, which was not measured. The effects of the model on sinkage and trim are qualitatively examined using hydrostatics. The hydrostatic estimates show good agreement with experimental data. The model is then implemented in a CFD code, CFDShip-Iowa 4.0. A baseline CFD simulation is carried out mimicking the towed bare hull condition, showing good quantitative agreement with EFD results especially with regards to resistance, $E=0.78\%$, and sinkage, $E=0.8\%$, and reasonably good agreement for trim, $E=14.3\%$. The CFD waterjet model is shown to be reasonably accurate in predicting resistance, $E<5\%$, sinkage, $E=9.0\%$, and trim, $E=13.7\%$, as the errors are comparable in magnitude to previous simulations using the code. However, the thrust deduction fraction $t$ from the simulations is positive whereas the data indicate negative $t$. Such application of the model will be useful for prediction of local flow variables which are difficult to measure in experiments. The ITTC procedures which already require extensive data collection could be extended to measure the input variables required for the CFD waterjet model. Pressure measurements at the inlet would allow for separately specifying $\Delta P_{in}A_{in}$ and $\Delta F_S$, instead of approximating $\Delta P_{in}A_{in}$ using the pressure at the vicinity of the inlet as was done for the current validation.

The model can also be used for powering predictions once waterjet flow input variable correlations are available based on CFD for the waterjet system and/or experimental data. Detailed waterjet flow simulation results from JHSS and DC were used along with available data for DTMB 5594 to derive correlations for the waterjet model input variables. Correlations obtained from this limited analysis indicate that this approach is feasible. However, additional detailed simulations and experiments for different waterjet/hull geometries over a wide range of operating conditions need to be investigated before such correlations can be fully established.
ACKNOWLEDGMENTS

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REFERENCES


Table 1: Errors in % Data from previous CFD Simulations using CFDShip-Iowa

<table>
<thead>
<tr>
<th>Scenario</th>
<th>Resistance</th>
<th>Sinkage</th>
<th>Trim</th>
</tr>
</thead>
<tbody>
<tr>
<td>5512 (Carrica et al., 2007b)</td>
<td>4.3</td>
<td>7.4</td>
<td>10.4</td>
</tr>
<tr>
<td>Towed Athena (Xing et al., 2008)</td>
<td>2.1</td>
<td>7.7</td>
<td>9.6</td>
</tr>
<tr>
<td>Propelled Athena (Xing et al., 2008)</td>
<td>4.5</td>
<td>8.1</td>
<td>5.0</td>
</tr>
<tr>
<td>HSSL-Delft Catamaran (Stern et al., 2006)</td>
<td>8</td>
<td>23</td>
<td>17</td>
</tr>
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</table>

Table 2. Boundary Conditions

<table>
<thead>
<tr>
<th>Boundary conditions</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>Inlet</td>
<td>((U, V, W) = (1,0,0), \partial P/\partial x = 0)</td>
</tr>
<tr>
<td>Exit</td>
<td>(\partial(U, V, W)/\partial x^2 = 0, \partial P/\partial x = 0)</td>
</tr>
<tr>
<td>No-Slip</td>
<td>((U, V, W) = 0, \partial P/\partial n = 0) (where (n) is normal to the boundary)</td>
</tr>
<tr>
<td>Symmetry</td>
<td>(\partial(U, W, P)/\partial x = 0, V = 0).</td>
</tr>
<tr>
<td>Far-field 1</td>
<td>(\partial(U, V, W)/\partial n = 0, P = 0)</td>
</tr>
<tr>
<td>Far-field 2</td>
<td>(\partial(U, V, W)/\partial n = 0, P = 0)</td>
</tr>
<tr>
<td>At free-surface interface</td>
<td>(\partial(U, V, W)/\partial n = 0, p = \frac{z}{Fr^2})</td>
</tr>
</tbody>
</table>

Table 3: Data for CFD waterjet model for 5594 based on Wilson et al. (2005)

<table>
<thead>
<tr>
<th>Geometry Variables</th>
<th>Flow Variables</th>
</tr>
</thead>
<tbody>
<tr>
<td>(A_{in} = \frac{A^*_n}{L_0^2} = (0,0,5.60 \times 10^{-4})),</td>
<td>(\dot{m} = \frac{\rho Q}{\rho U_0 L_0^2} = 1.207 \times 10^{-4})</td>
</tr>
<tr>
<td>(A_6 = \frac{A^*_6}{L_0^4} = (8.21 \times 10^{-5},0,0))</td>
<td>(\Delta F_x + \Delta P_{in} A_{in} = (0,0,-6.35 \times 10^{-5}))</td>
</tr>
<tr>
<td>(r_R = \frac{r^*_R}{L_0} = (4.837 \times 10^{-1},0,-3.994 \times 10^{-3}))</td>
<td>(\Delta W_f = (0,0,-6.213 \times 10^{-7}))</td>
</tr>
<tr>
<td>(r_m = \frac{r^*_m}{L_0} = (-1.997 \times 10^{-2},0,-6.753 \times 10^{-3}))</td>
<td>(\alpha = 0^\circ, R_x = R_x^* / \rho U_0^2 L_0^2 = 8.767 \times 10^{-5})</td>
</tr>
<tr>
<td>(r_6 = \frac{r^*_6}{L_0} = (3.994 \times 10^{-3},0,0))</td>
<td>(c_{MinX} = 1.0594, c_{MinZ} = 1.06, c_{M6} = 1.019)</td>
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<tr>
<td>(r_{AFS} = \frac{r^*_{AFS}}{L_0} = (4.57 \times 10^{-1},0,-1.01 \times 10^{-2}))</td>
<td>(\overline{V}<em>{in} = \overline{V}</em>{in}^* / U_0 = (0.730,0,0.216))</td>
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<tr>
<td>(r_{AFY} = \frac{r^*_{AFY}}{L_0} = (1.005 \times 10^{-3},0,2.744 \times 10^{-3}))</td>
<td>(\overline{V}_6 = \overline{V}_6^* / U_0 = (1.47,0,0))</td>
</tr>
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Table 4: Model parameters for DTMB Model 5594 as used in Wilson et al. (2005)

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Value</th>
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<tr>
<td>Density, $r$</td>
<td>1000 kg/m$^3$</td>
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<tr>
<td>Kinematic Viscosity, $n$</td>
<td>1×10^{-6} m$^2$/s</td>
</tr>
<tr>
<td>Waterline length, $L_0$</td>
<td>6.956 m</td>
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<tr>
<td>Design speed, $U_0$</td>
<td>4.218 m/s</td>
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<tr>
<td>Froude number, $Fr$</td>
<td>0.511</td>
</tr>
<tr>
<td>Static wetted area, $A_S$</td>
<td>3.722 m$^2$</td>
</tr>
<tr>
<td>Waterplane area (Miller, 2007), $A_{WP}$</td>
<td>2.463 m$^2$</td>
</tr>
<tr>
<td>Longitudinal moment of inertia, $I_L$</td>
<td>6.239 m$^4$</td>
</tr>
</tbody>
</table>

Table 5: Waterjet induced forces and moments

<table>
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<tr>
<th></th>
<th>$R_X$</th>
<th>$M_Z$</th>
<th>$\Delta F_{SZ} + \Delta P_{in}A_{inz}$</th>
<th>$M_{WJ}$</th>
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<tbody>
<tr>
<td>CFD-WJM</td>
<td>-8.767×10^{-5}</td>
<td>2.755×10^{-5}</td>
<td>-6.35×10^{-5}</td>
<td>1.597×10^{-5}</td>
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Table 6: Results of predicted total resistance, sinkage, and trim for the towed and self-propelled simulation

<table>
<thead>
<tr>
<th>Cases</th>
<th>$C_{TX}$</th>
<th>$-R_X+F_D$</th>
<th>$E$ ($%$D)</th>
<th>$\sigma$ ($z/L_0$)</th>
<th>$E$ ($%$D)</th>
<th>$\tau$ (rad)</th>
<th>$E$ ($%$D)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Towed Barehull</td>
<td>EFD</td>
<td>1.4288×10^{-4}</td>
<td>-</td>
<td>-1.438×10^{-3}</td>
<td>-</td>
<td>6.35×10^{-3}</td>
<td>-</td>
</tr>
<tr>
<td></td>
<td>CFD</td>
<td>1.4176×10^{-4}</td>
<td>-</td>
<td>+0.78</td>
<td>-1.427×10^{-3}</td>
<td>+0.8</td>
<td>5.44×10^{-3}</td>
</tr>
<tr>
<td>Towed Propelled</td>
<td>EFD</td>
<td>-</td>
<td>1.3870×10^{-4}</td>
<td>-1.682×10^{-3}</td>
<td>-</td>
<td>7.91×10^{-3}</td>
<td>-</td>
</tr>
<tr>
<td></td>
<td>CFD-WJM</td>
<td>1.4507×10^{-4}</td>
<td>-</td>
<td>-4.6</td>
<td>-1.527×10^{-3}</td>
<td>+9.0</td>
<td>6.82×10^{-3}</td>
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</table>

Table 7: Waterjet induced sinkage $\Delta \sigma$ and trim $\Delta \tau$

<table>
<thead>
<tr>
<th>Cases</th>
<th>$\Delta \sigma$ ($z/L$)</th>
<th>$\Delta \sigma / Draft$ %</th>
<th>$E$ ($%$D)</th>
<th>$\Delta \sigma / \sigma_{BH}$ %</th>
<th>$\Delta \tau$ (rad)</th>
<th>$E$ ($%$D)</th>
<th>$\Delta \tau / \tau_{BH}$ %</th>
</tr>
</thead>
<tbody>
<tr>
<td>EFD</td>
<td>-2.44×10^{-4}</td>
<td>0.90</td>
<td>-</td>
<td>16.97</td>
<td>1.56×10^{-3}</td>
<td>-</td>
<td>+24.57</td>
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<tr>
<td>Hydrostatic Est.</td>
<td>-1.84×10^{-4}</td>
<td>0.70</td>
<td>-22.2</td>
<td>13.10</td>
<td>1.562×10^{-3}</td>
<td>-1.3</td>
<td>+24.60</td>
</tr>
<tr>
<td>CFD-WJM model Predictions</td>
<td>-1×10^{-4}</td>
<td>0.37</td>
<td>-58.9</td>
<td>7.01</td>
<td>1.38×10^{-3}</td>
<td>+11.5</td>
<td>+25.51</td>
</tr>
</tbody>
</table>
Fig. 1 ITTC Waterjet model control volume

Fig. 2 CFD Waterjet model control volume

Fig. 3 Forces and moments on a towed ship model: a) Bare-hull simulation; and b) Waterjet-propelled simulation
Fig. 4 Overset grid design and boundary conditions

Fig. 5 $C_P$ on the model afterbody
Fig. 6 Contours of bare hull axial velocity upstream of the waterjet inlets at $x/L=0.96$

Fig. 7 Forces and motions: (a) Bare hull $C_{TX}$ and self propelled $R_X$ for three different hull forms, (b) thrust deduction, (c) Sinkage and (d) Trim
Fig. 8 Vertical forces: (a) Vertical forces vs. Fr, (b) Vertical forces vs. IVR, (c) Vertical force components ratios variation with IVR
Fig. 9 Inlet flow angles: (a) $\Phi$ vs. IVR (b) $\Phi/|\Phi|$ vs. IVR

Fig. 10 Momentum correction factors at $A_{in}$
Fig. 11 Correlation of vertical force coefficients